



**ELECTRONIC CASH CONTROLLED BY
NON-HOMOMORPHIC SIGNATURES**

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Background Of The Invention

Field Of The Invention

The present invention generally relates to a method and system to create and manage
10 digital cash.

Prior Art

A review of digital cash and other forms of electronic payment systems can be found
in D. O'Mahony, M. Peirce, and H. Tewari: Electronic Payment Systems (Artech
15 House, Boston, 1997). The basic idea of electronic cash is that a digitally signed
statement of value from a bank can be redeemed by the bank as no one else can
produce such a statement, as long as the bank keeps track of the statements it has
already redeemed. To protect the beneficiary of the statement, encryption will be used
in communication, or the delivery has to be made by conventional delivery methods.
20 This basic principle however does not allow for anonymity, which is often considered
as one of the main virtues of cash. To overcome this difficulty, David Chaum (D.
Chaum "*Blind Signature System*", Advances in Cryptology: Proceedings of Crypto 83,
Plenum Press, New York, 1984, Pages 153—153) has proposed to use blind signature,
which uses the homomorphic property of the RSA protocol for public signature.

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This idea has been the starting point of actual use of electronic cash, as offered by the
Mark Twain Bank of St. Louis, Missouri for some time starting October 1995. The
fact that this operation was not continued is most probably due to the fact that
electronic commerce (or e-commerce) was not yet developed enough. The growth of
30 e-commerce as we witness it now will certainly ask for some forms of electronic cash
to be available. It is thus important to provide ways to generate and manage electronic

cash which would have all the virtues, and avoid the weaknesses, of the solutions originally offered.

One approach to address this need is to use a digital signature Sign . The main property of a digital signature Sign such as RSA which is used for blind signatures is

5 the fact that Sign has some interesting algebraic properties:

1) it is a homomorphism, i.e., $\text{Sign}(kx) = \text{Sign}(k)\text{Sign}(x)$,

2) it is possible to create pairs $r, \text{Sign}(r)$

for a random message r . More precisely, anyone can choose $\text{Sign}(r)$ at random and then compute r as the function Sign^{-1} is known publicly.

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The basic idea is as follows. Customer C will choose a message x which is going to be the coin. Also, C will generate a pair, $k, \text{Sign}(k)$, for a random number k . C sends the product kx to the bank B which will compute $\text{Sign}(kx)$. B then sends $\text{Sign}(kx)$ to

15 C , using, for instance, a public encryption scheme provided by C , or using some session key exchanged between C and B using a Diffie-Hellman session, or using some other form of communication such as delivery on a diskette transported by an armored carrier. C can then compute $\text{Sign}(x)$ by simply dividing $\text{Sign}(kx)$ by $\text{Sign}(k)$.

The pair $(x, \text{Sign}(x))$ is now redeemable by B , at a value usually determined by the signature being used, and B cannot recognize C when some payee P presents $(x,$
20 $\text{Sign}(x))$, as the knowledge of kx does not allow practical recognition of x nor of $\text{Sign}(x)$.

The main problem with the approach described above is that a signature scheme with properties (1) and (2) described above is clearly not secure. Indeed property (2) says
25 that it is easy to forge signatures on random messages. Property (1) says that after seeing the signatures on two messages x_1 and x_2 , it is easy to compute the signature on the message $x = x_1x_2$. In order to overcome this problem, valid messages are required to have a special "structure" (e.g., the message x must be encoded using the PKCS#1 standard for digital signature). The hope is that messages with this structure
30 are sparse and hard to forge even given properties (1) and (2) (since messages with

that structure will not appear with a significant probability). However, this is simply a hope and is not a proven mathematical property of the signature scheme or of the encoding. The drawback is that it may be possible to discover an algorithm to forge messages even when we restrict them to this structured sparse set.

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A *provably secure* signature scheme instead has the property that even after seeing several signed messages, it is not possible to produce a different valid message. This is a mathematical property of the signature scheme which is proven under some reasonable computational assumption (say the hardness of factoring large integers).

- 10 Provably secure schemes are known in the cryptographic literature, but for none of them is it known how to create a blinding mechanism.

Summary Of The Invention

- 15 An Object of this invention is to improve cryptography methods and systems.

Another object of the present invention is to provide a method and apparatus to create and manage electronic cash using possibly a non-homomorphic signature scheme.

- 20 A further object of this invention is to provide a mechanism to create digital cash which does not use blinding and relies on provably secure signature schemes.

- Another object of the present invention is to provide a method and system to emit and circulate secure electronic cash that allows to use non-homomorphic signature
25 schemes, and avoids having to use blind signature techniques.

A further object of this invention is to provide a method and system to emit and circulate secure electronic cash that allows to use non-homomorphic signature schemes and avoids having to use blind signature techniques, and where the

generation of the electronic cash is performed using secure cryptographic hardware that protects its keys from everyone, including the owners.

These and other objective are attained with a method and system for establishing and
5 managing digital cash. This method is to emit and circulate secure electronic cash that
allows to use non-homomorphic signature schemes, and avoids having to use blind
signature techniques. With one specific embodiment, the method provides anonymous
digital cash, and comprises the steps of providing an entity with a secure coprocessor,
a user establishing a secure channel to a program running on said coprocessor, and the
10 user sending a coin to be digitally signed to the coprocessor.

Brief Description Of The Drawings

The foregoing and other objects, aspects and advantages will be better understood
15 from the following detailed description of a preferred embodiment of the invention
with reference to the drawings, in which:

Figure 1 illustrates an IBM 4758 PCI Cryptographic coprocessor, which may be used
in the practice of this invention.
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Figure 2 is a block diagram that also represents the main flows needed for the
preferred embodiment of the present invention.

Detailed Description Of The Preferred Embodiments

25 The present invention builds on a pair of technologies: (1) a secure cryptography
generator such as the IBM 4758 PCI Cryptographic Coprocessor; and (2)
Cryptography.

30 The IBM 4758 PCI Cryptographic Coprocessor:

The IBM 4758 PCI Cryptographic Coprocessor is a programmable, field upgradeable piece of secure hardware that has a general purpose computational power about equivalent to a personal computer from the early 90's. It performs high speed cryptographic operations, and provides secure key storage. It is both

5 cryptographically secure and able to detect and protect itself against physical attacks (probe, voltage, temperature, radiation). It is in fact one of the only two devices that are **Federal Information Processing Standard (FIPS) 140-1** overall 4 certified (hardware and microcode: certificate #35), the other one coming integrated in IBM 390 mainframes (the IBM CMOS Cryptographic Coprocessor: certificate #40) while

10 the price of an IBM 4758 is about a couple of thousand dollars. The IBM 4758 is indeed a popular PCI bus interface for servers, and can serve as device driver for NT, AIX, OS/2, Linux, and OS/390.

Typical use of cryptographic coprocessors such as the IBM 4758 or some smart cards

15 include High Speed Bulk Cryptography (for instance for digital movies, in-flight entertainment systems, secure databases, confidential video-conferences, telemedicine, telecommuting, etc.) and Security in Non Trusted Environments (for instance, for smart card personalization, electronic currency dispensers, electronic benefits transfer, server-based smart card substitutes, home banking, certification authorities, secure

20 database key control, e-postage meters, electronic payments, secret algorithms, secure time stamps, contest winner selection, software usage metering, electronic securities trading, hotel room gaming, etc.).

Cryptography

25 The use of Private key/public key pairs (or SK/PK pairs; we also say public schemes) as means to encrypt or digitally sign a file or document, of secret encoding keys, and of secure hash functions (such as SHA-1, as fully specified in the Federal Information Processing Standard Publication 180-1) are now well known. A description of these techniques with directions on how to use several of their implementations can be

found in "Handbook of applied Cryptography", by Alfred J. Menezes, Paul C. van Oorschot and Scott A. Vastone, CRC Press, 1997.

To fix the ideas, we recall that a digital signature scheme is used in the form of a pair
5 of functions Sign and Sign^{-1} which are inverse of each other, i.e., for a message X to
be signed, $\text{Sign}^{-1}(\text{Sign}(X))=X$. The function Sign is kept secret, being known only to
some legitimate owner of the signature and his/her agents. The function Sign^{-1} is
known publicly, and accessible for instance through the World Wide Web (WWW),
through some agency specializing in providing PKI, or given away by the owner of the
10 pair to whoever needs to check the identity of the sender and/or that a message is
exactly as the owner intended it to be.

We also recall that a public encryption scheme is used in the form of a pair of
functions Encr and Encr^{-1} which are the inverse of each other, i.e., for a plain text X to
15 be signed, $\text{Encr}^{-1}(\text{Encr}(X))=X$. The function Encr^{-1} is kept secret, being known only
to some legitimate owner of the signature and his/her agents. The function Encr is
known publicly, and accessible for instance through the WWW or through some
agency specializing in providing PKI, or given away by the owner of the pair to
whoever wants to send the owner a secret message, or keep secret some part of the
20 message.

Probably the most often used public schemes (to generate and use a SK/PK pair in
order to allow for public encryption or digital signature) are the Rivest-Shamir-
Adleman.(RSA) protocols. Several other methods could also be used (see, e.g., the
25 "Handbook of applied Cryptography"). In the case when the functions Sign and Sign^{-1}
(or Encr^{-1} and Encr) are produced according to the RSA protocol, it is now preferred
to use at least 1024 bits for X and $\text{Sign}(X)$ (the formerly often used 512 bits are no
more considered as secure).

The RSA scheme works as follows. The signer (let us call him Bob) chooses two large primes P, Q (say 512 bits long) and sets $n = PQ$. Then he chooses a small prime number e which is relatively prime to both $P-1$ and $Q-1$. This property guarantees that there exist a number d such that for any k , $k^{ed} \bmod n = k \bmod n$.

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Bob sets (n,e) as his public key and keeps d secret as well as P and Q . The signature for a message X is $S_x = \text{Sign}(X) = X^d \bmod n$.

And it can be verified by checking that $S_x^e = X \bmod n$.

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Clearly the RSA scheme has the homomorphic property $\text{Sign}(kx) = \text{Sign}(k)\text{Sign}(x)$.

Also it is possible to generate random pairs $(r, \text{Sign}(r))$: simply choose a random integer R smaller than n and then set

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$$R = \text{Sign}(r), \text{ and } r = R^e \bmod n.$$

As discussed earlier, these are the properties that allow for *blind signature*.

Mathematically, the blind signature protocol using RSA works as follows. Alice wants Bob to sign message x but without him knowing that he signed it for her. This is accomplished in three easy steps:

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1. Alice chooses a *blinding factor*, k , as a random number between 1 and n , and *blinds* x by computing $U = xk^e \bmod n$.

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2. Bob signs U as $U^d = (xk^e)^d \bmod n = x^d k^{ed} \bmod n = x^d k \bmod n$.

3. Alice unblinds U^d by computing the signature of x as

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$$\text{Sign}(x) = U^d / k = (x^d k \bmod n) / k = x^d \bmod n.$$

- In electronic cash application, Bob is the bank B, and will need to keep track of all pairs $(x, \text{sign}(x))$ which have been redeemed. To keep databases bounded, expiration dates will be associated to any signature. Notice that in order for this to be a valid
- 5 blinding mechanism, x must follow some special structure (for example, follow the PKXS#1 standard for digital signatures). Pairs $(x, \text{Sign}(x))$ in which x does not follow the prescribed structure are not valid coins (otherwise Alice could easily generate coins on her own).
- 10 Golwasser, Micall, Rivest ("*A Digital Signature Scheme Secure Against Chosen-Message Attack*", SIAM J. On Computing, Vol.17, no.2, pp. 281-308); and Dwork, Naor ("*An Efficient Existentially Unforgeable Signature Scheme and Its Applications*", J. Of Cryptology, Vol.11, No.3, pp.187-208) among others, have recognized that the homomorphic property of RSA is a potential source of weakness. They also proposed
- 15 new signature schemes that are provably secure, i.e., in which it is provably impossible (under some reasonable computational assumption) to forge signatures. Other, more efficient, provably secure protocols have been proposed, for instance by Gennaro, Halevi, Rabin ("*Secure Hash-and-Sign Signatures Without the Random Oracle*", EUROCRYPT'99, pp. 123-139, Springer LNCS vol. 1592) or Cramer,
- 20 Shoup ("*Signature schemes based on the Strong RSA Assumption*", Proc. 6th ACM Conf. on Computer and Communications Security, 1999).

As a message may contain much more information than the length of the keys, several methods can be used, possibly concurrently, as is well known in the art. For instance,

25 one can split the message in several pieces, some or all of which will be signed, or one can compress the information, for instance using a secure hash function, or one can select a subset of the information, etc. Clearly, the protocol which is chosen has to be known publicly if one desires to use public key cryptography.

Notice that even if one wishes to uses the benefits of public key cryptography, it may be useful to also hide secret information in the messages, so that one could recognize that someone has succeeded in breaking the keys being used. As usual in the art, it is advisable to change the keys being used every so often, depending on the application,
5 and to keep a list of former keys.

Another important enabler of secure electronic communication is the possibility to exchange secret keys while exchanging only messages which can be understood by third parties. Several protocols have been created to this effect such as Diffie-
10 Hellman.

The preferred embodiment of the present invention uses a secure cryptographic generator such as the IBM 4758 PCI Cryptographic Coprocessor to create and manage electronic cash using possibly a non-homomorphic signature scheme. Preferably, the
15 secure cryptography generator has the following properties, something which can be achieved by the 4758:

Prop1: it has a public key signature $(\text{Sign1}, \text{Sign1}^{-1})$, whose secret part Sign1 cannot be obtained by anyone, except
20 possibly by very special attacks which cannot be unnoticed, (no such attack has been proven to succeed so far on the 4758),

Prop2: it can perform standard encryption, say some list List1 of them, once provided keys to that effect; once provided an encryption scheme ES in List1 and an associated
25 key $k(\text{ES})$, and a request to sign a certificate in some prescribed format Cert, corresponding to an amount that belong to a list List2, it will only accept to provide the signature $\text{Sign}(\text{Cert})$ after encryption using the method ES and the key $k(\text{ES})$ - the clear form of $\text{Sign}(\text{Cert})$ cannot be obtained by anyone, except by very special attacks which cannot be unnoticed (again, no such attack has been proven to succeed so far on
30 the 4758).

Some extra properties can be imposed for some embodiments of the invention, some of which will be listed later, but Prop1 and Prop2 are the basic properties we assume each time we speak of a secure cryptography generator.

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When ordering cash, customer C communicates to the secure cryptography generator SCG at the bank B (preferably using some secure channel on which both SCG and B can read), its own public encryption scheme (method belonging to List1, and key, all together denoted as Encr2), and orders some cash amount, with a description of the way to cut the amount into units, in a way compatible with List2 (for instance List2 will comprise all amounts available with regular coins and bills in the currency of interest to the customer). Each unit, Unit, is signed by the secure cryptography generator, and the signature Sign1(Unit) is then encrypted as Encr2(Sign1(Unit)) by SCG using the customer's public encryption scheme.

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The SCG also computes Encr2(Unit). Besides the value, Val(Unit), of the unit, and preferably an expiration date, Exp(Unit), Unit comprises a large random number generated by SCG, in such a way that the same number will never reappear in further transactions, and possibly a secret version of that number provided by SCG, using a very secure method such as a one time pad. The SCG then communicates the quadruple

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$(\text{Val}(\text{Unit}), \text{Exp}(\text{Unit}), \text{Encr2}(\text{Unit}), \text{Encr2}(\text{Sign1}(\text{Unit})))$

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to the computer system of the bank. After payment of Val(Unit) and fees, B communicates the quadruple to C, and keeps it in its database until some expiration date that C knows and accepts beforehand (unused electronic cash can be substituted back to regular cash, or to electronic cash with later expiration date, possibly for a fee). The communication from SCG to C through B allows to guarantee the delivery of the quadruple in case of crash of one of the machines involved and/or the

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communication lines. It also allows C to ask for a copy of the quadruple if it is later lost before use.

C will later use the electronic cash by offering the pair $(Unit, Sign1(Unit))$ as payment.

- 5 The recipient of the pair can check with B the validity of the pair. Once a pair has been redeemed, Unit is kept in the database of B until expiration of its validity, to avoid repeated use by C or any other party.

- 10 Notice that when a recipient presents $(Unit, Sign1(Unit))$ to B for credit, it is not possible for B to link this signed coin to the customer C who withdrew it in the first place. Indeed at withdrawal time, all the bank B saw was the encrypted value $Encr2(Unit)$, $Encr2(Sign1(Unit))$ and this does not allow in practice recognition of the decrypted values.

- 15 Traditional electronic cash management functions, such as replacement of electronic cash coming close to expiration by an electronic wallet held at C's location can be used as with former forms of electronic cash.

- 20 The advantages of the present method comprises the following properties:
-any signature scheme, in particular provably secure ones such as Cramer-Shoup, can be used for $Sign1$.

- supplementary encryption, possibly more secure or more efficient than public key, can be used by the SCG, which is useful in particular for large value units,

- 25 -the same signature can be used for different amounts as Unit may allow for this freedom, within List2,

- the bank is better protected from possibly corrupt employees.

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One of the important modifications which can be made is to use multiple signatures, provided by some set of SCGs instead of a single one. For instance, five machines could sign, and the electronic cash would be accepted as soon as three signatures at least are legitimate.

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Besides examining the pairs (Unit, Sign1(Unit)) as unique verification, B can also be asked to accept Unit as one it has produced. This has the advantage of extra security for B. This step cannot be done if the SCG is destroyed, but identically programmed backups can be provided, and this is an extra step of security anyhow.

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Also, although perhaps less preferred, the SCG may be authorized to print out the list of Units it has generated and their signatures using Sign1, after a sufficient number of operations have been made. In fact, several SCG's could arrange to print out their combined lists every so often.

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With reference now to Figure 2, at 100 we have represented the customer C, at 200 we have represented the bank B, which has one or more secure cryptography generators (SCG), possibly in the form of 4758 machines, at 210, one or more databases at 220, one or more payment systems at 230, one or more computer systems at 240, at 300 we have represented some seller with whom C will want to use the electronic cash.

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The bank acquires the SCG's from some vendor, such as IBM for the IBM 4758. The machines may have property Prop3 below, besides Prop1 and Prop2:

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Prop3: it has a public key encryption scheme (Encr1, Encr1⁻¹), whose secret part Encr1⁻¹ cannot be obtained by anyone, except possibly by very special attacks which cannot be unnoticed (once more we recall that, so far, no such attack has been proven to succeed so far on the 4758).

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This will allow several machines to have the same keys without the keys to be compromised. The machines can also this way share one time pads, and other cryptographic function. Instead of Prop3, the machines can also communicate by building session key, for instance using the Diffie-Hellman protocol. When we speak
5 of a SCG, we speak either of a single machine, or a series of them working in a coordinated way, as a multi-component single machine. The invention does not depend on the distinction between these two cases.

When the customer wants to buy electronic cash from B, it composes a message 105
10 comprising

1. the description of the order, according to some format communicated or posted by B,
2. the public key of its own public key encryption scheme (together with the
15 designation of that scheme: C will check that this scheme belongs to those in List1 that can be handled by the bank's SCG).

C then sends this message to the bank, and it reaches the SCG at 210.

20 The SCG then generates the quadruple (Val(Unit), Exp(Unit), Encr2(Unit), Encr2(Sign1(Unit))) which is stores in the database 220.

After C pays at 230, the value Val(Unit), or a collection of them, depending on the original order 105, B sends to C the pair

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$$(Encr2(Unit), Encr2(Sign1(Unit)))$$

at 115. From this pair C (and C only in a reasonable time) can compute the clear pair

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$$(Unit, Sign1(Unit))$$

at 125 that will later be used, e.g., with some seller at 300. When the seller, or whoever else, is proposed the pair 125 as payment, it will check validity with B. B will use computer system 240 to check the cryptographic validity of the message, and
5 database 220 to check that the Unit has not yet been used. If the pair is valid, payment is made to 300: for instance its account belonging to 300 is made. B then store Unit in the database until expiration at least.

While it is apparent that the invention herein disclosed is well calculated to fulfill the
10 objects stated above, it will be appreciated that numerous modifications and embodiments may be devised by those skilled in the art, and it is intended that the appended claims cover all such modifications and embodiments as fall within the true spirit and scope of the present invention.